

Electrical Circuits Lab. 0903219

Series RC Circuit Phasor Diagram

- Simple steps to draw phasor diagram of a series RC circuit without memorizing:

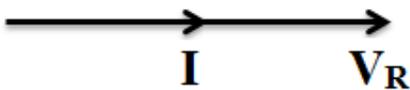
* Start with the quantity (voltage or current) that is common for the resistor R and the capacitor C , which is here the source current I (because it passes through both R and C without being divided).

Step1



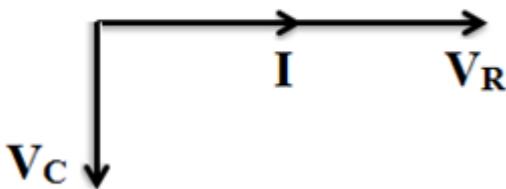
* Now we know that I and resistor voltage V_R are in phase or have the same phase angle (there zero crossings are the same on the time axis) and V_R is greater than I in magnitude.

Step2



* Since I equal the capacitor current I_C and we know that I_C leads the capacitor voltage V_C by 90 degrees, we will add V_C on the phasor diagram as follows:

Step3



* Now, the source voltage V_S equals the vector summation of V_R and V_C :

Step4

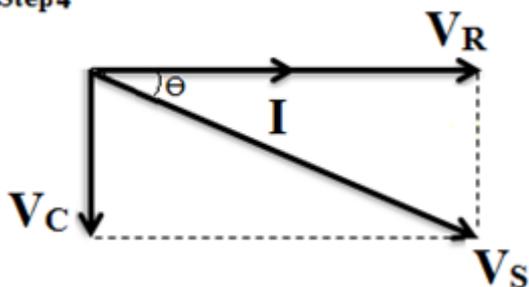


Figure (2) Series RC circuit Phasor Diagram

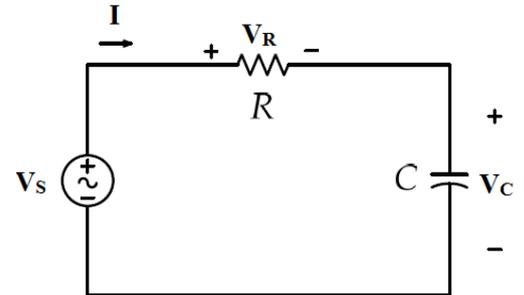


Figure (1) Series RC circuit

- Important notes on the phasor diagram of series RC circuit shown in figure (2):

A- All the vectors are rotating in the same angular speed ω .

B- This circuit acts as a capacitive circuit and **I** leads **V_S** by a phase shift of Θ (which is the current angle $\angle \mathbf{I}$ if the source voltage is the reference signal).

Θ ranges from 0° to 90° ($0^\circ < \Theta < 90^\circ$). If $\Theta=0^\circ$ then this circuit becomes a resistive circuit and if $\Theta=90^\circ$ then the circuit becomes a pure capacitive circuit.

C- The phase shift between the source voltage and its current Θ is important and you have two ways to find its value:

a-
$$\Theta = \tan^{-1} \frac{V_C \text{ (imaginary part of } VS)}{V_R \text{ (real part of } vs)}$$

b-
$$\Theta = \angle \mathbf{I} = - \angle \mathbf{Z} = - \tan^{-1} \frac{1/\omega C \text{ (imaginary part of } Z)}{R \text{ (real part of } Z)}$$

D- Using the phasor diagram, you can find all needed quantities in the circuit like all the voltages magnitude and phase and all the currents magnitude and phase.

For a series **RC** circuit, if the magnitude of **V_C** and **V_R** was measured in Lab. (as a peak value from an oscilloscope or rms value from a digital multimeter), then we can find the magnitude of **V_S** as follows:

$$|V_S| = \sqrt{|V_C|^2 + |V_R|^2}$$

E- You can find all leading or lagging voltages and currents in this circuit with respect to a reference signal like the source voltage **V_S**.

For example, it is clearly shown by the phasor diagram that **I** leads **V_S** by Θ degrees, **V_R** leads **V_S** by Θ degrees (since it is in phase with **I**) and **V_C** lags **V_S** by $90^\circ - \Theta$.

F- The phasor diagram helps in finding the change in current and voltage (magnitude and phase) with voltage source frequency **f** changing.

With frequency **f** increasing, the capacitive reactance **X_C** will decrease and **V_C** will decrease too, the the resistor **R** will not be affected by the change of **f**, then by voltage

division rule V_R will increase (to prevent V_S from changing since V_S is a voltage source). Since X_C decrease and R is constant the total impedance Z will decrease and the source current I will increase. $\angle I$ and $\angle Z$ will decrease because $\angle I = -\angle Z = \theta = \tan^{-1} \frac{V_C}{V_R} = -\tan^{-1} \left(\frac{1}{\omega C R} \right)$ and the \tan^{-1} function is increasing on the interval from 0 to 90° .

In a concise way:

$$f \uparrow \mid X_C \mid \downarrow \mid Z \mid \downarrow \mid I \mid \uparrow \mid V_R \mid \uparrow \mid V_C \mid \downarrow \mid \theta \mid \downarrow .$$

G- Figure (3) below shows a time domain representation for all the vectors shown on the phasor diagram:

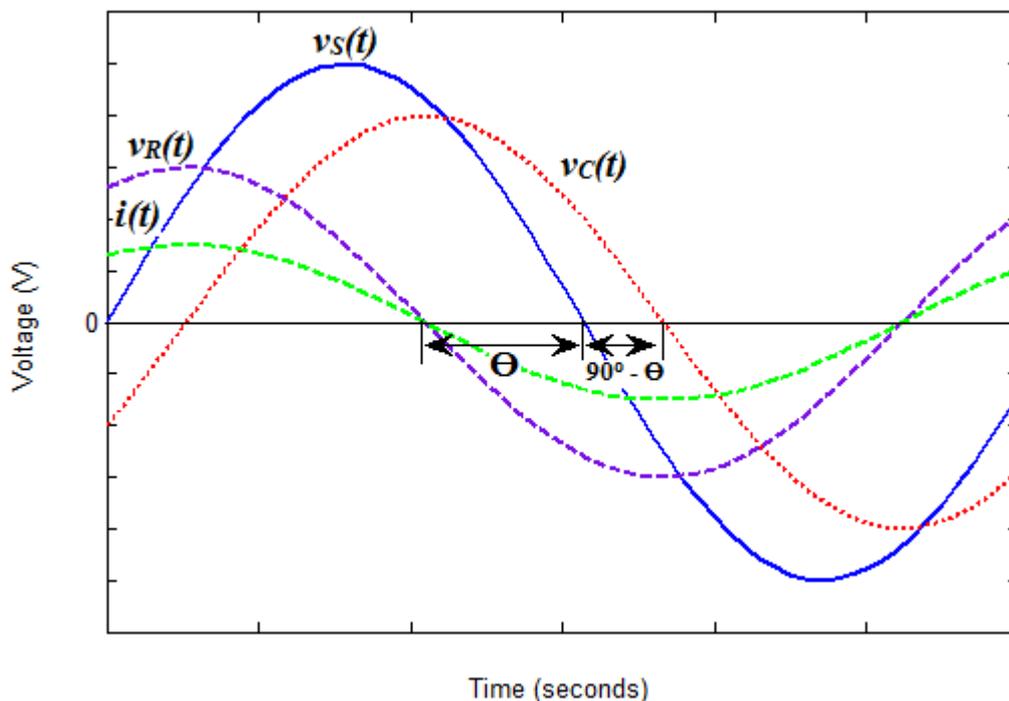


Figure (3) Series RC Circuit Time Domain Representation

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Parallel RC Circuit Phasor Diagram

- Simple steps to draw phasor diagram of a parallel RC circuit without memorizing:

* Start with the quantity (voltage or current) that is common for the resistor R and the capacitor C , which is here the source Voltage V_s (because it is parallel with both R and C without being divided).

Step1

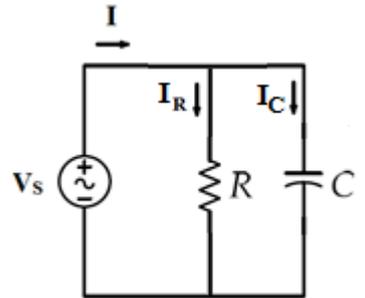
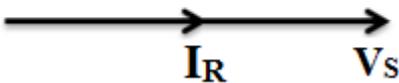


Figure (1) Parallel RC

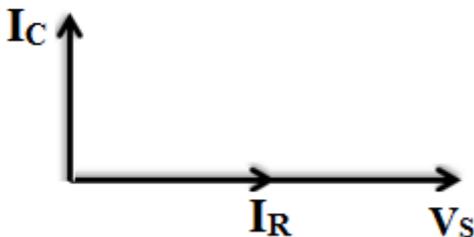
* Now we know that resistor current I_R and resistor voltage V_R (which equals V_s) are in phase or have the same phase angle (there zero crossings are the same on the time axis) and V_R is greater than I_R in magnitude.

Step2



* Since V_s equal the voltage V_C and we know that V_C lags the capacitor current I_C by 90 degrees, we will add I_C on the phasor diagram as follows:

Step3



* Finally, the source current I equal the vector summation of I_R and I_C :

Step4

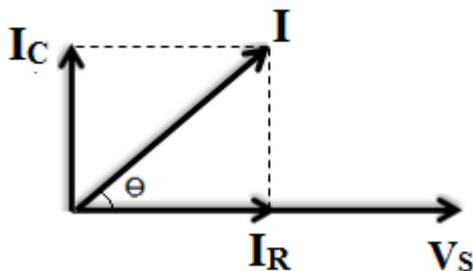


Figure (2) Parallel RC circuit Phasor Diagram

- Important notes on the phasor diagram of Parallel RC circuit shown in figure (2):

A- All the vectors are rotating in the same angular speed ω .

B- This circuit acts as a capacitive circuit and \mathbf{I} leads \mathbf{V}_S by a phase shift of Θ (which is the current angle $\angle \mathbf{I}$ if the source voltage is the reference signal).

Θ ranges from 0° to 90° ($0^\circ < \Theta < 90^\circ$). If $\Theta=0^\circ$ then this circuit becomes a resistive circuit and if $\Theta=90^\circ$ then the circuit becomes a pure capacitive circuit.

C- The phase shift between the source voltage and its current Θ is important and you have two ways to find its value:

$$\Theta = \tan^{-1} \frac{I_C \text{ (imaginary part of } V_S)}{I_R \text{ (real part of } V_S)}$$

$$\Theta = \angle \mathbf{I} = \angle \mathbf{Y} = \tan^{-1} \frac{B_C \text{ (imaginary part of } Y)}{G \text{ (real part of } Y)}$$

D- Using the phasor diagram, you can find all needed quantities in the circuit like all the voltages magnitude and phase and all the currents magnitude and phase.

For a parallel **RC** circuit, if the magnitude of \mathbf{I}_C and \mathbf{I}_R was measured in Lab. (as a peak value from an oscilloscope or rms value from a digital multimeter), then we can find the magnitude of \mathbf{I} as follows:

$$|\mathbf{I}| = \sqrt{|\mathbf{I}_C|^2 + |\mathbf{I}_R|^2}$$

E- You can find all leading or lagging quantities in this circuit with respect to a reference signal like the source voltage \mathbf{V}_S .

For example, it is clearly shown by the phasor diagram that \mathbf{I} leads \mathbf{V}_S by Θ degrees, \mathbf{I}_R lags \mathbf{I} by Θ degrees and \mathbf{I}_C leads \mathbf{I} by $90^\circ - \Theta$.

F- The phasor diagram helps in finding the change in quantities (magnitude and phase) with voltage source frequency f changing.

With frequency f increasing, the capacitive reactance X_C will decrease and so I_C will increase, the the resistor R will not be affected by the change of f and I_R will not change with frequency. Since X_C decrease and R is constant the total impedance Z will decrease, the source current I will increase and the admittance Y will increase. $\angle I$ and $\angle Y$ will increase because $\angle I = \angle Y = \theta = \tan^{-1} \frac{I_C}{I_R} = \tan^{-1} \frac{\omega C}{1/R}$ and the \tan^{-1} function is increasing on the interval from 0 to 90° .

In a concise way:

$f \uparrow |X_C| \downarrow |Z| \downarrow |Y| \uparrow |I| \uparrow |I_C| \uparrow \theta \uparrow |I_R| \text{constant.}$

G- Figure (3) below shows a time domain representation for all the vectors shown on the phasor diagram:

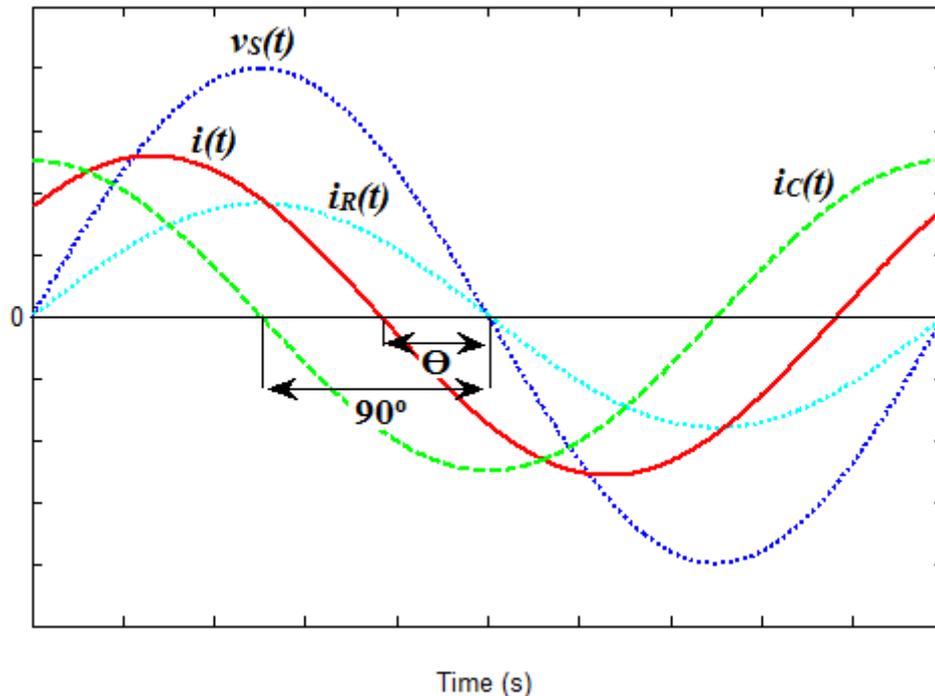


Figure (3) Parallel RC Circuit Time Domain Representation